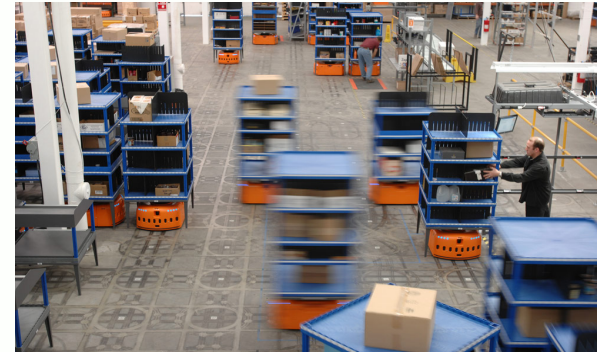


Introduction

- **Why multi-robot system?**
 - Better global system performance
 - More abilities
 - More robustness
 - Lower cost
- **What is multi-robot coordination?**

A team of robots interacting with others to reach a common goal.



Kiva Systems



Robocup

Introduction

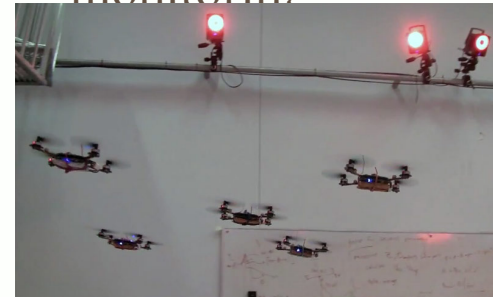
- Why building efficient multi-robot coordination is difficult?

Most problems are *NP-hard*:

- Multi-robot Task Allocation
 - Resource allocation
 - Exploration
- Multi-robot Motion Planning
 - Routing
 - Trajectory planning



Wildfire
monitoring



Multi-UAV path planning

Introduction

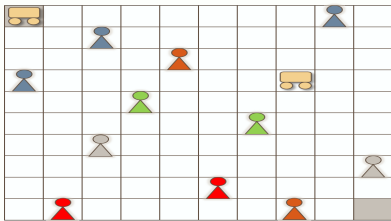
- How to reduce the difficulty?
 - Reduce the environment space
 - Reduce the action space
 - Estimate a finite horizon of future

Outline

- Known Environment with Global Communication:

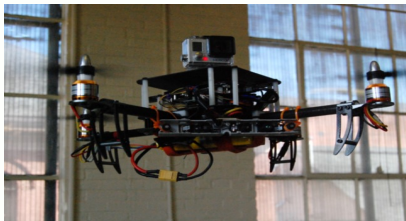


Intelligent In-Orchard Bin-Managing System For Tree Fruit Harvest



Multi-robot Routing for Dynamic Information Gathering

- Unknown Environment with Limited Communication:



Multi-UAV Explore, Map, and Search in Unknown Environments

Intelligent In-Orchard Bin-Managing System for Tree Fruit Harvest



(aka. the Bin-dog project)



Motivation

- High labor demand of tree fruit(apple) harvest
- Low productivity with inefficient bin management



Main Goal

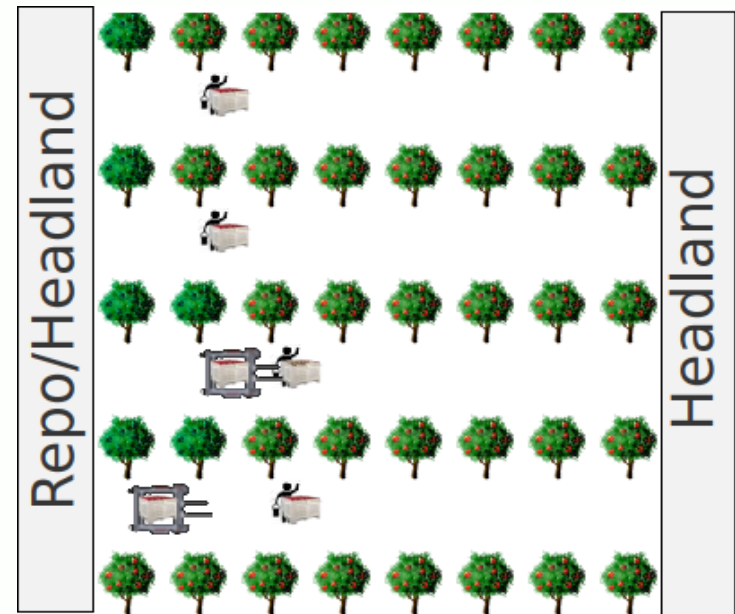
To develop an intelligent bin-managing system supported by a robotic self-propelled fruit bin carrier



“Bin-dog”, designed by Center for Precision & Automated Agriculture Systems,
Washington State University

Simulation Environment

- 10 trees x 5 lanes
- Workers cost 2 steps to finish one tree
- Robots move 1 step per time when carrying a full bin, 2 steps otherwise.



Simulation Setup

- Groups of workers are initialized in the beginning of the lanes.
- No more apples?
 - Workers move to a new location.
 - Workers request a new bin.
- Robots choose which bin to pick up.
 - Robots wait if the target bin is not full yet.
- Robots choose where to carry a new bin to.

Algorithm: Baseline (Naive Greedy)

- Greedy, no coordination.
- Choose the closest full bin.
- Choose the earliest requested location.
- Choose the bin that will be filled faster.
 - Wait if the target bin is not full.
- Priority: other robots cannot see a chosen bin/request.



Not efficient!

Algorithm: Auction-based

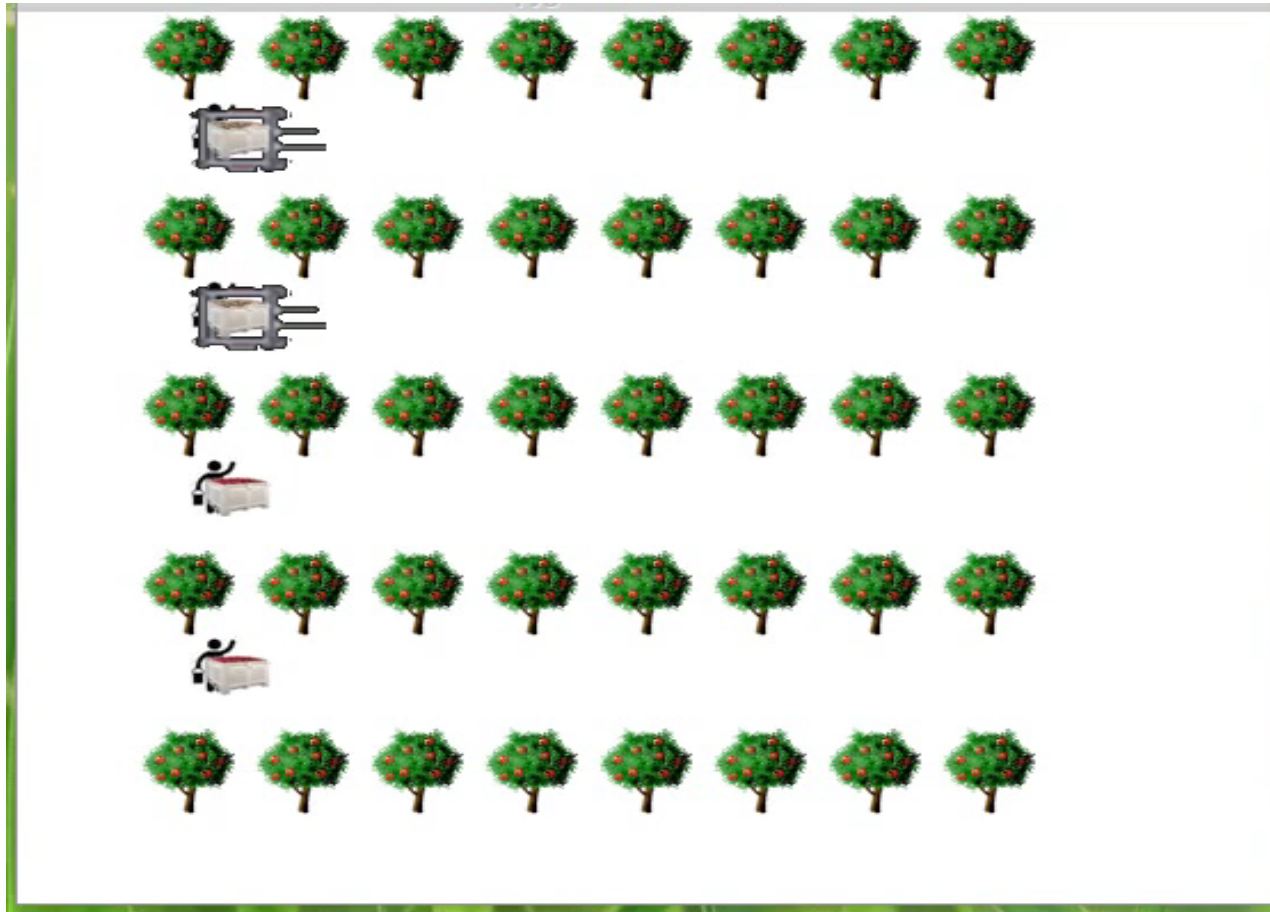
- Robots coordinate through auction.
 - Each robot makes plans to pick up a bin.

- Plan cost:

$$C = t_T + t_W$$

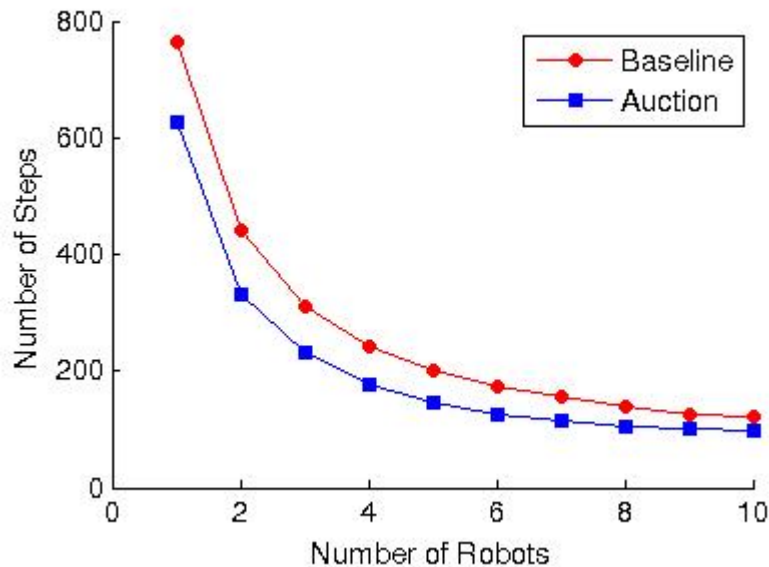
- t_T : the time required to reach target bin.
 - t_W : the time required to wait for target bin to be full.
- The one with least cost wins the task

Simulation (Auction-based)



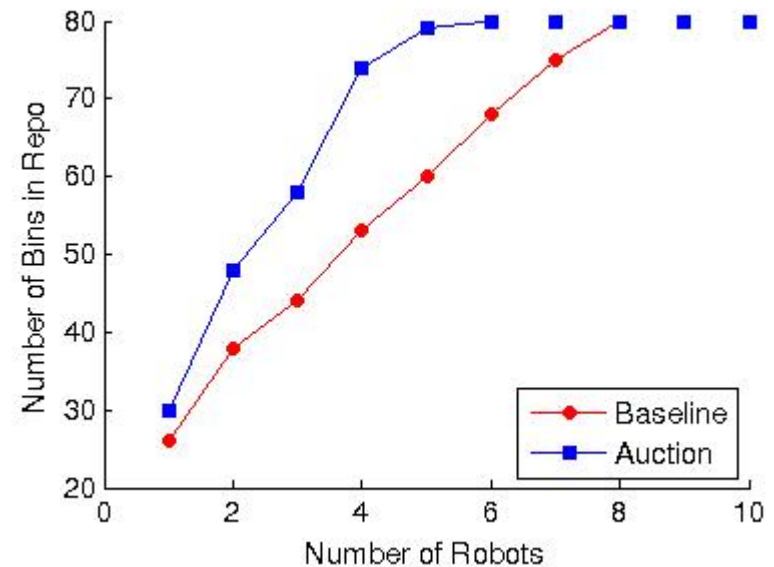
Results

Total steps cost to finish all the tasks (80 bins)



Lower is better

Number of bins retrieved after 150 time steps



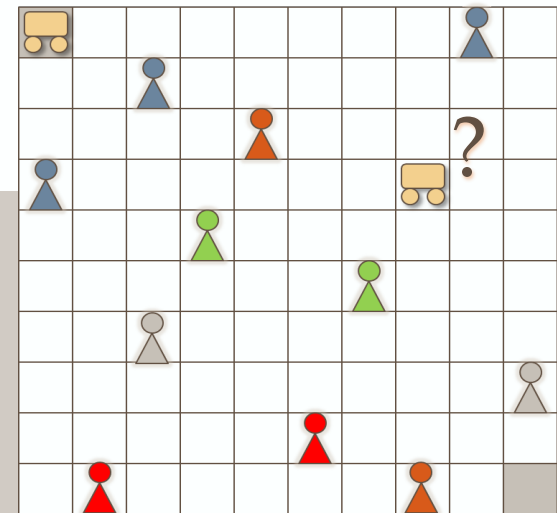
Higher is better

Extension

“Bin-dog” is interesting, but...

- Visit multiple points of interest one time?
- How to balance the workload between robots?
- Workers work in different speed?

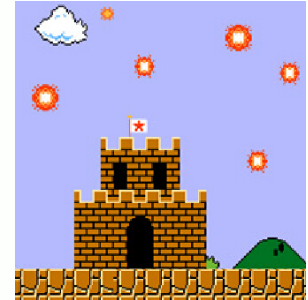
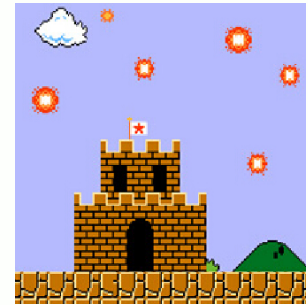
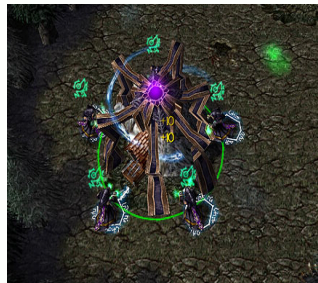
Multi-Robot Routing for Information Gathering



Introduction

Goal

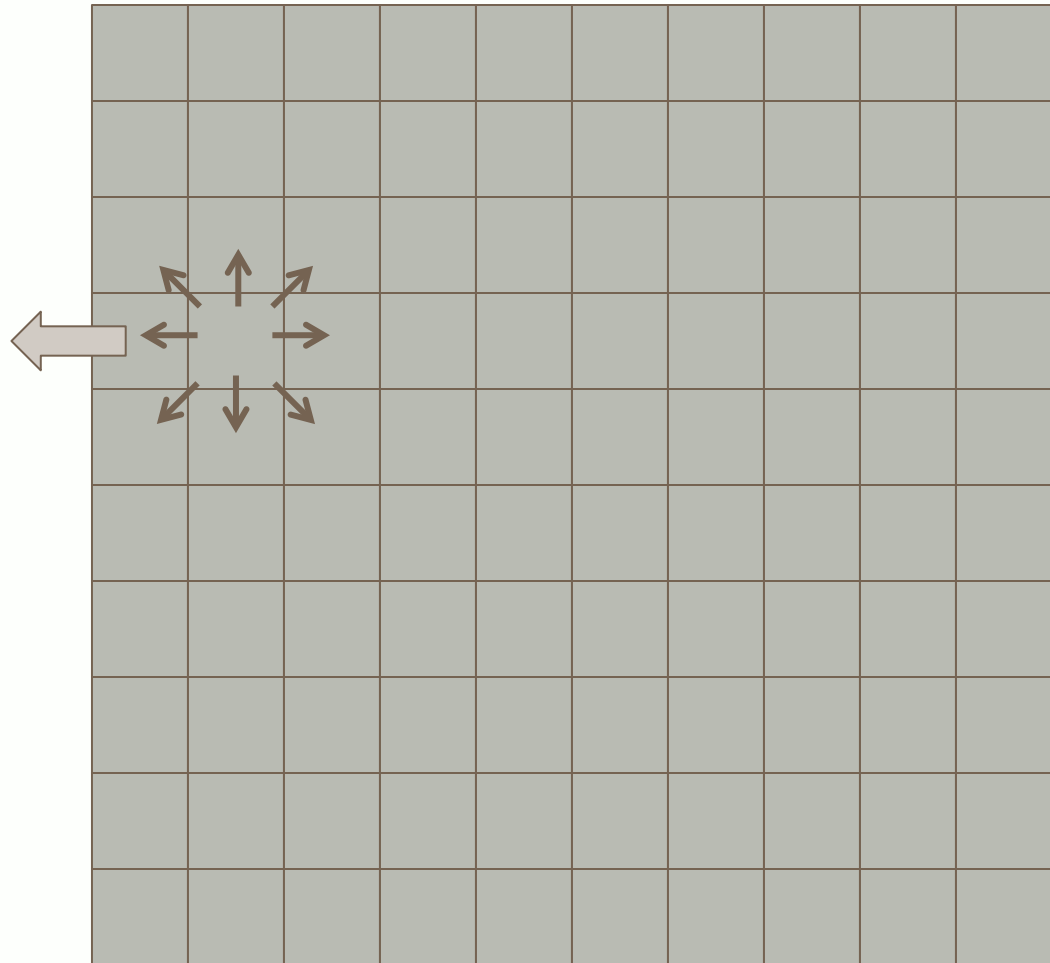
Coordinate a team of robot to retrieve resources from a number of resource collectors in a static environment.



Introduction

Informative map

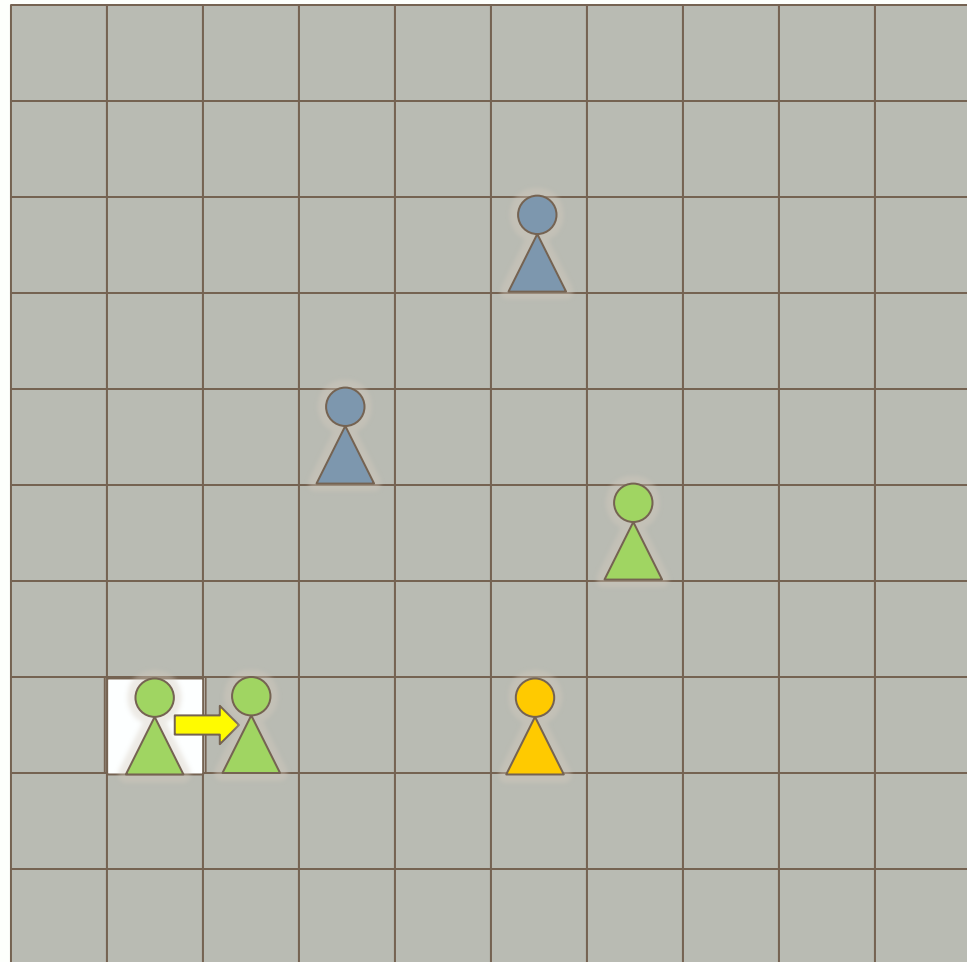
- 8-connected 2D grid
- No obstacles
- Each cell has a certain amount of information



Introduction

Collectors:

- Collect information from each cell
- Move to a neighbor cell when finish
- Individual collecting rate
- Limited capacity, pause when full

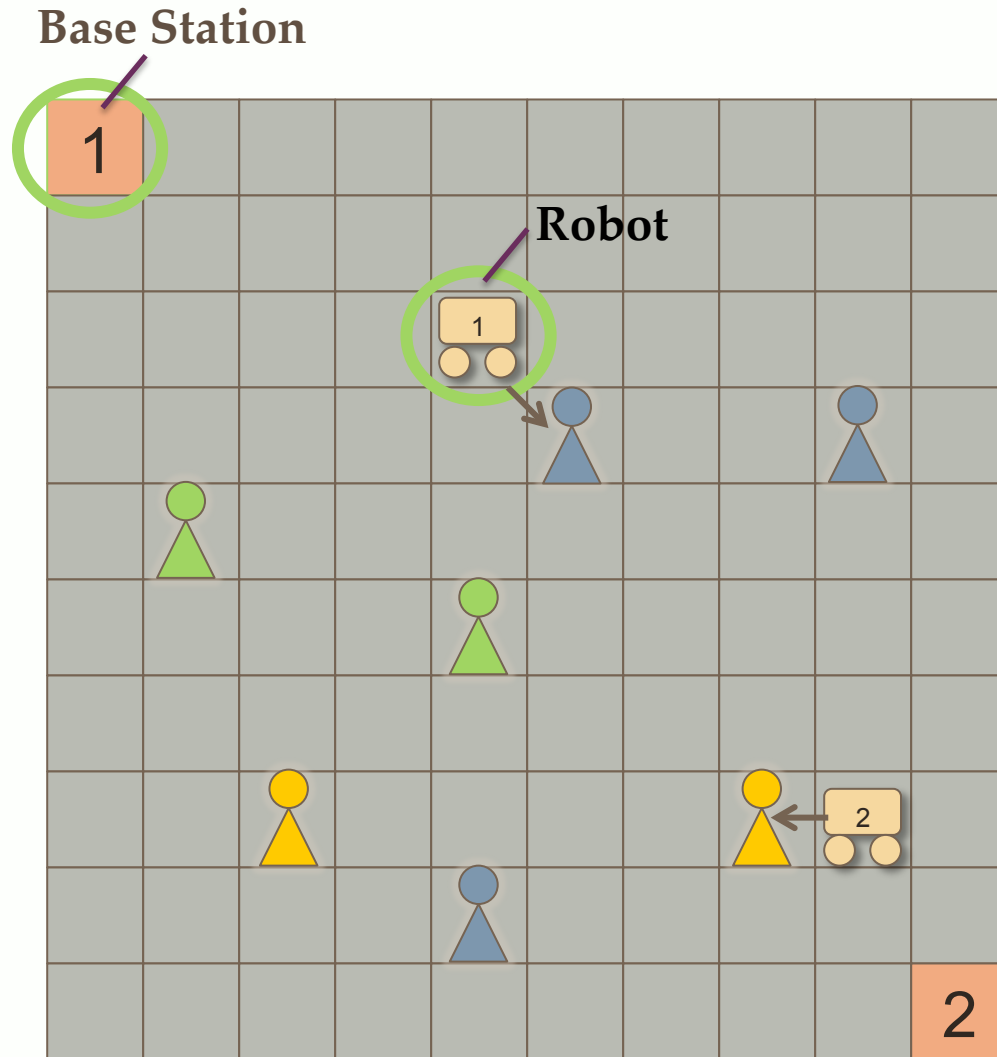


Introduction

Robots

- Visit collectors to retrieve information
- Consistent speed
- Different base stations
- Limited capacity, go back if full

Robot can retrieve
a portion of
information from each
collector



Problem Formulation

- **Given:**

- **n collectors**
- **m robots**

- **Objective Function**

$$\operatorname{argmax}(\neg p \downarrow i \in \Psi \operatorname{Info}(R \downarrow i \dots m) - \operatorname{Idle}(T \downarrow i \dots n))$$

Sub-problems

- **Two sub-problems**
 - **Multi-robot Task allocation:**
 - which collector should be assigned to which robot?
 - **Multi-robot Motion Planning:**
 - Visit the goal collectors in which order?
 - Retrieve how much information from a specific collector?

Algorithm:

Sequential Auction with Greedy Path Planning

- **Task Allocation: Sequential Auction**

- Sort the unassigned tasks (collectors) by *urgency*:

$$U \downarrow i = (\text{collecting rate} + \text{current fullness}) / \text{distance}$$

- Auction tasks based on urgency

- Cost of each robot:

$c \downarrow i$ = total travel distance of current tasks + distance from last task to the auctioning task

- Reassign if any robot idle

Demo:

Sequential Auction with Greedy Path Planning

Be *exact* full after visit
all assigned collectors

$$U \downarrow 1 > U \downarrow 2$$

$$T = 11$$

Information

Collected Estimation:

$$I = (r \downarrow 1 + r \downarrow 2) * T$$

+ *CUR*
Information

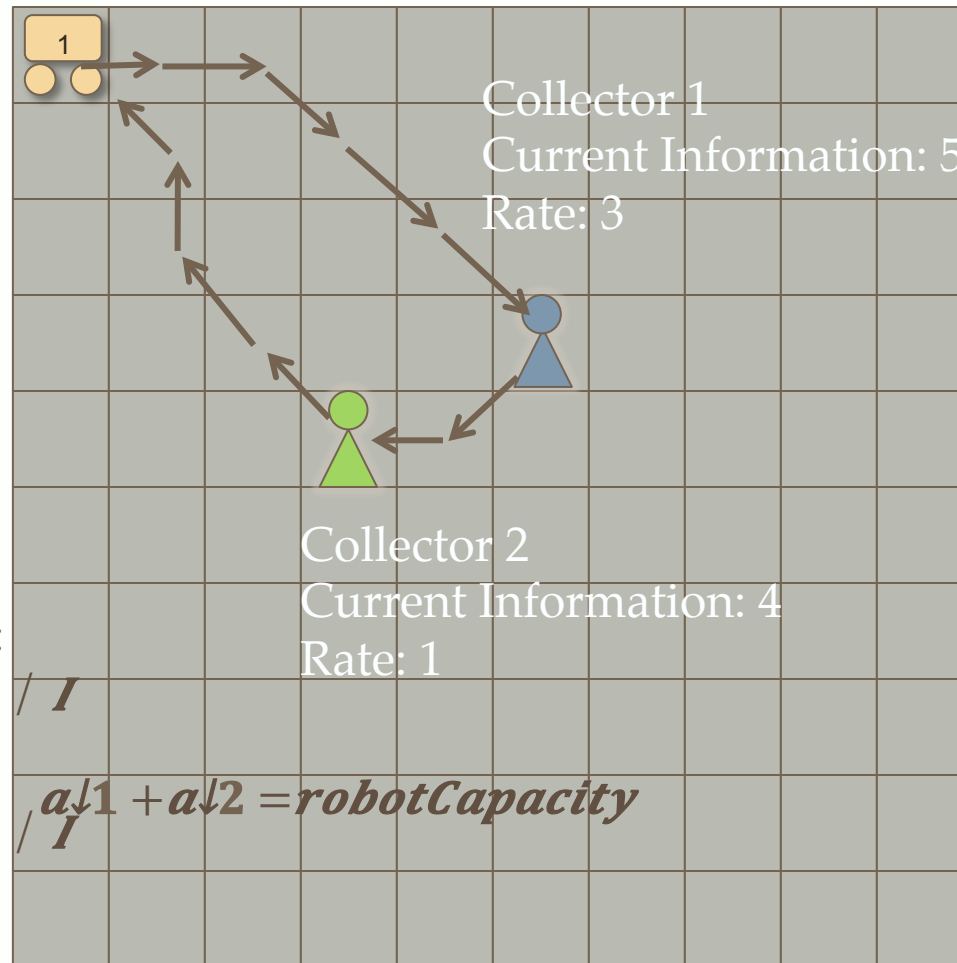
Retrieve for collector 1:

$$a \downarrow 1 = (r \downarrow 1 * T + cur \downarrow 1) / I$$

* robotCapacity

$$a \downarrow 2 = (r \downarrow 2 * T + cur \downarrow 1) / I$$

* robotCapacity



Algorithm:

Sequential Auction with Greedy Path Planning

- **Motion Planning: Greedy**

- **Path Planning** : 1-horizon greedy. Visit the most urgent collector first.

- **Information Gathering Planning**

- T : time *required* to travel the path.

- Estimated information collected by collector i :

$$\Delta \downarrow i = \text{content} \downarrow i + T \times f \downarrow i$$

- Amount to take (Try to be **exact** full after visit all assigned collectors):

$$a \downarrow i = \Delta \downarrow i / \sum_{j=1}^{|P|} \Delta \downarrow j \times \text{RobotCapacity}$$

Algorithm:

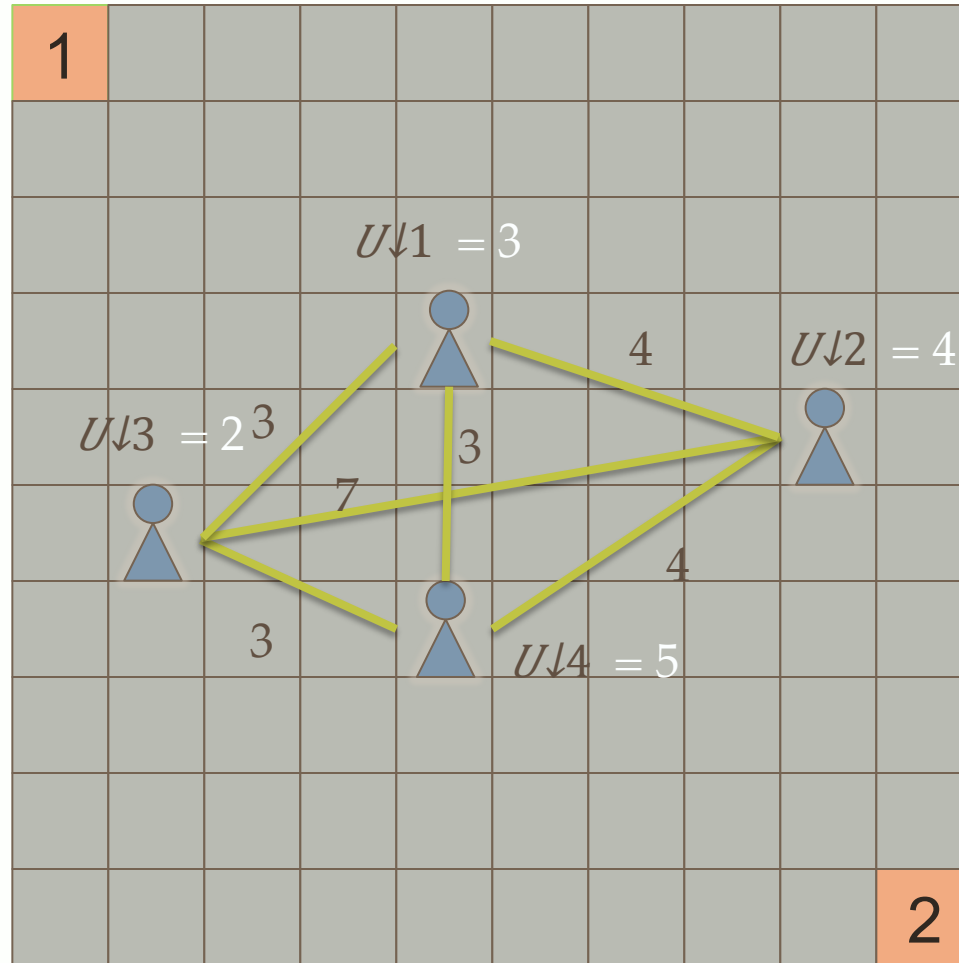
Distributed Sampling with RH-based Path Planning

- **Task allocation:** distributed sampling.
 - **Goal:** evenly distribute the workload to the robots

Demo:

Distributed Sampling with RH-based Path Planning

Create fully connected
Graph G



Demo:

Distributed Sampling with RH-based Path Planning

Random part it into m parts.

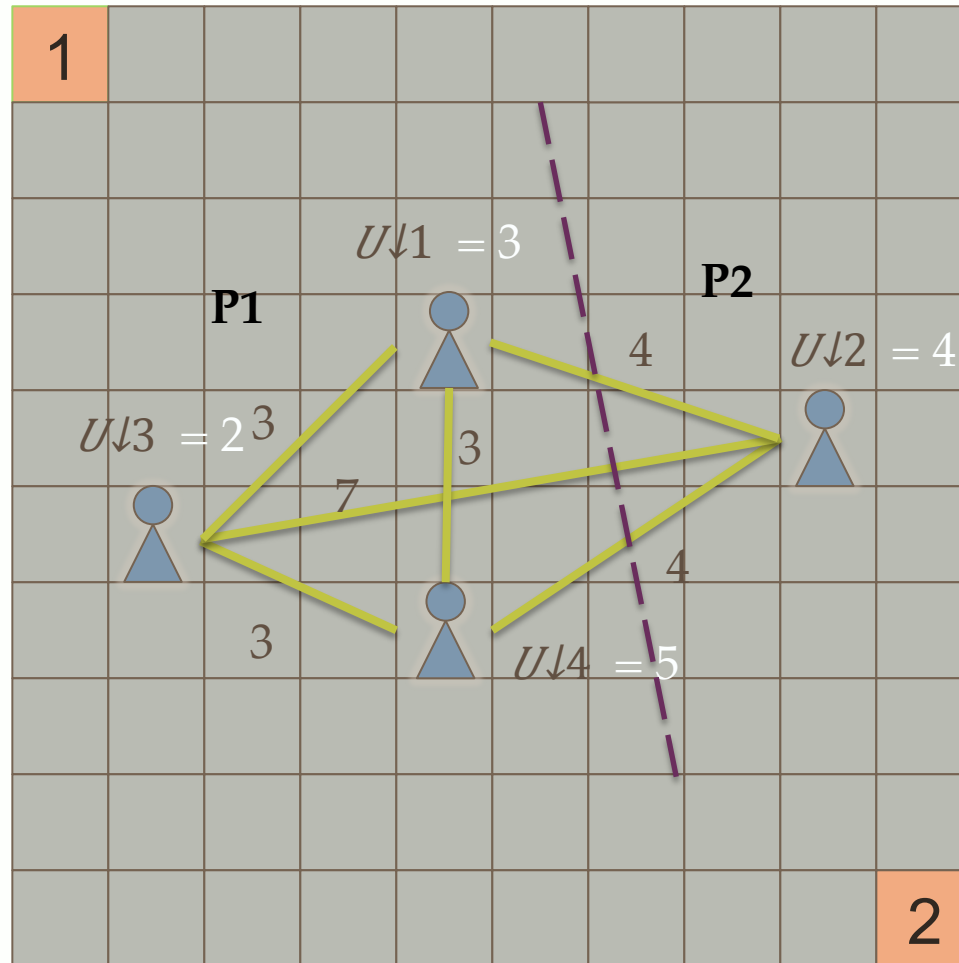
$$\text{Cost}(P1) = \text{sum}(U \downarrow 1, 3, 4)$$

$$+ \text{sum}(E \downarrow 13, 14, 34)$$

$$= 19$$

$$\text{Cost}(P2) = 4$$

$$\text{Diff}(P1, P2) = 15$$



Demo:

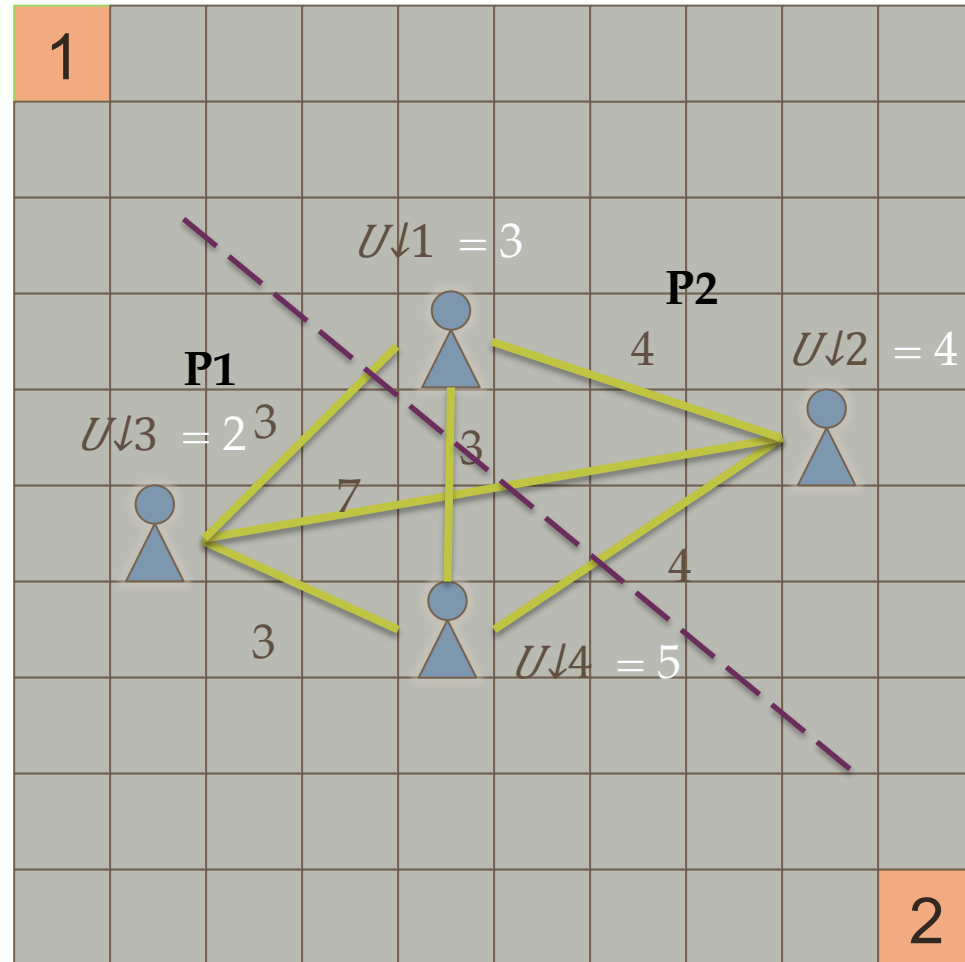
Distributed Sampling with RH-based Path Planning

Balance by move the
boundary nodes.

$$\text{Cost}(\text{P1}) = 10$$
$$\text{Cost(P2)} = 9$$

Diff(P1, P2) = 1 < previous Diff15

A better partition!



Demo:

Distributed Sampling with RH-based Path Planning

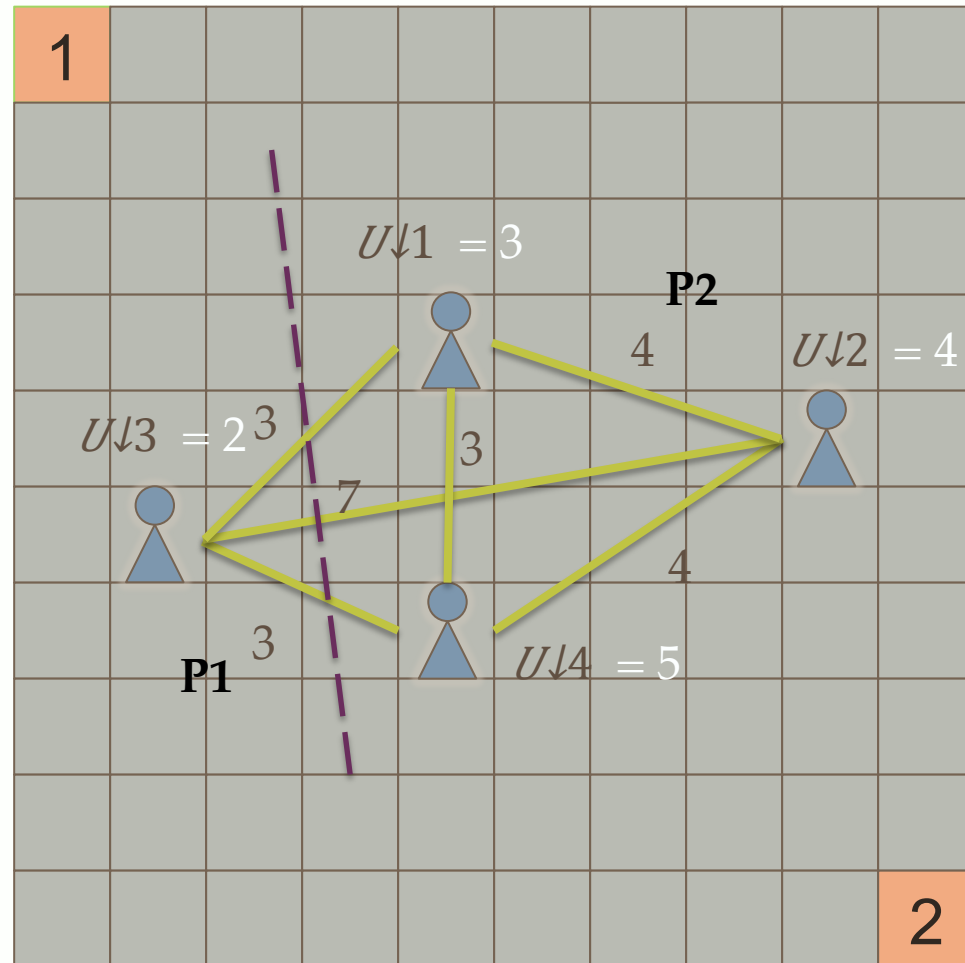
Balance by move the
boundary nodes.

$$\text{Cost}(P1) = 2$$

$$\text{Cost}(P2) = 23$$

$$\text{Diff}(P1, P2) = 21 > 1$$

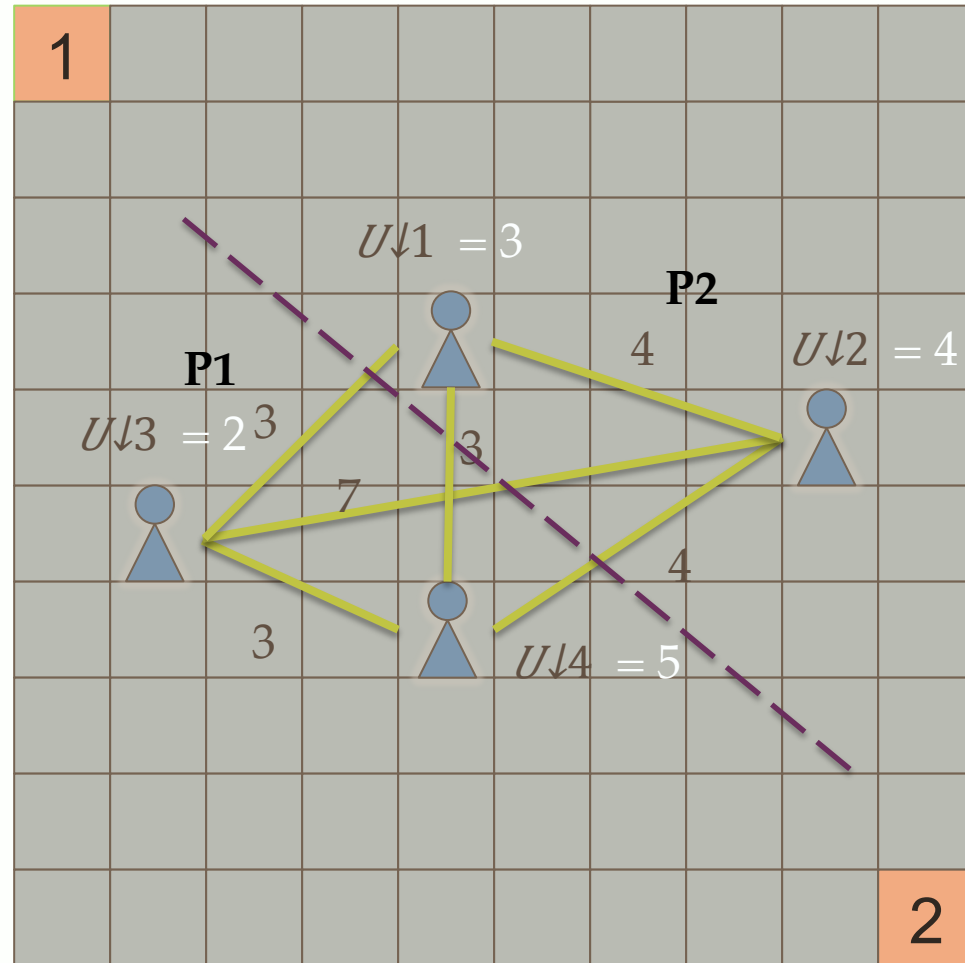
↑
previous Diff



Demo:

Distributed Sampling with RH-based Path Planning

Continue until converged



Workload Partition

Steps:

- Create a fully connected graph $G = (V, E)$
- V is the set of all nodes (collectors), E is the set of edges.
- Optimization problem:

$$\arg \min_{(G_i, G_j)} \left[\max_{i \in [1, m]} \left(\sum_{\forall a, b} (w_{v_a}^i + w_{e_b}^i) \right) - \min_{j \in [1, m]} \left(\sum_{\forall c, d} (w_{v_c}^j + w_{e_d}^j) \right) \right].$$

Time required
to reach capacity
Collector's fill rate

$$w_{v \downarrow a} = -t_{v \downarrow a} + f_{v \downarrow a}$$

$$w_{e \downarrow b} = \text{length}(e \downarrow b)$$

Proposed Algorithm:

Distributed Sampling with RH-based Path Planning

- **Routing**

- Receding Horizon-based routing.
- Look ahead h steps.

- Preferences of visiting a node v_i :

$$c \downarrow i = U \downarrow i / d \downarrow i$$

- $d_i = \text{dist}(R, v_i)$ if v_i is the first node in the path
- $d_i = \text{dist}(v_j, v_i)$ otherwise

Receding Horizon Path Planning

Find which collector
to visit first

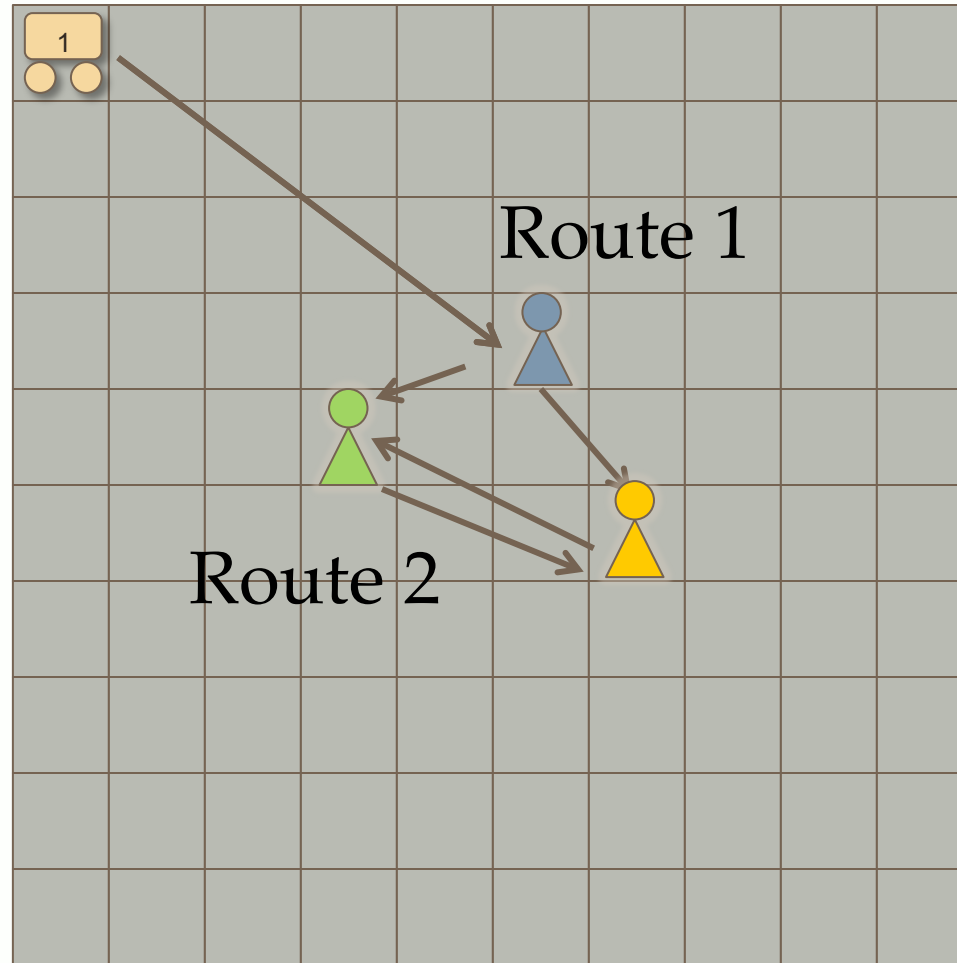
3-horizon planning

Route 1

Route 2

...

Route 6



Proposed Algorithm: Distributed Sampling with RH-based Path Planning

- Information Gathering Planning

- T : time *required* to travel the path.

- Estimated information collected by collector i :

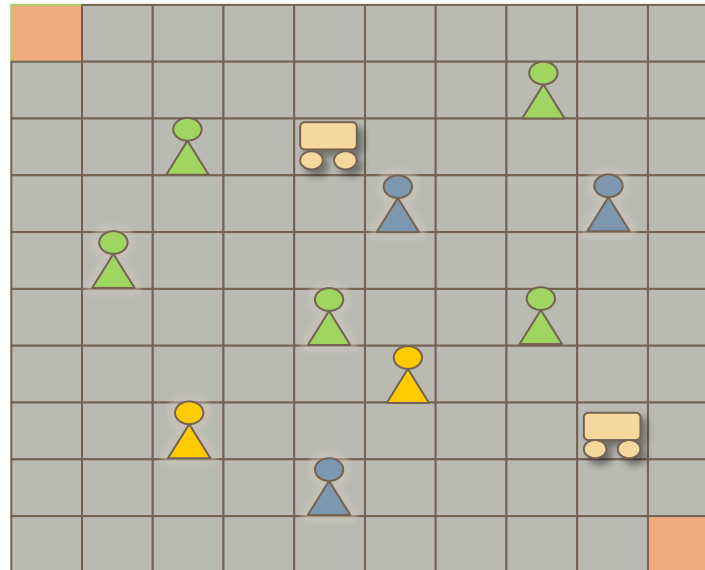
$$\Delta_i = \text{content}_i + T \times f_i$$

- Amount to take (Try to be **exact** full after visit all assigned collectors):

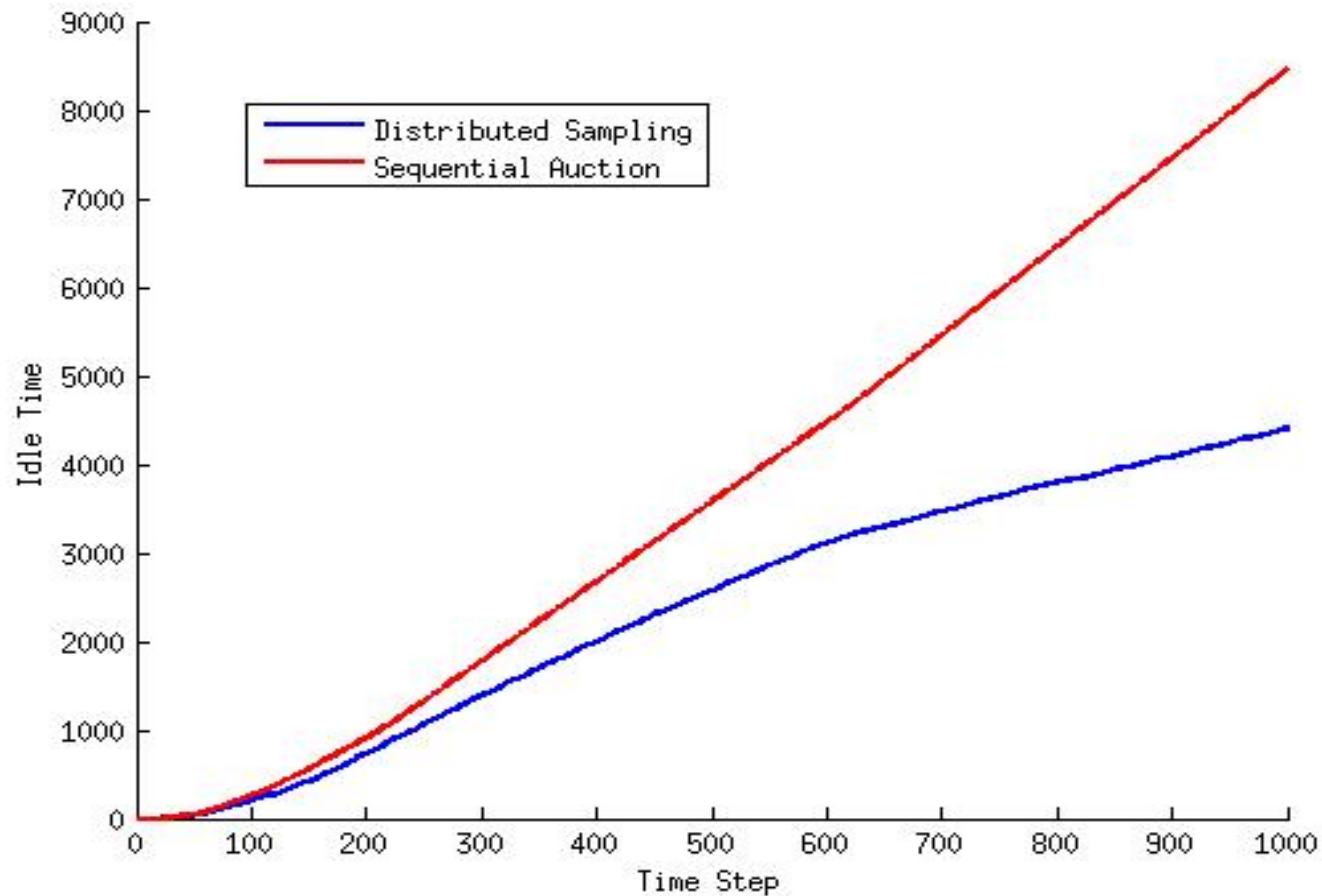
$$a_i = \Delta_i / \sum_{j=1}^{|P|} \Delta_j \times \text{RobotCapacity}$$

Simulation

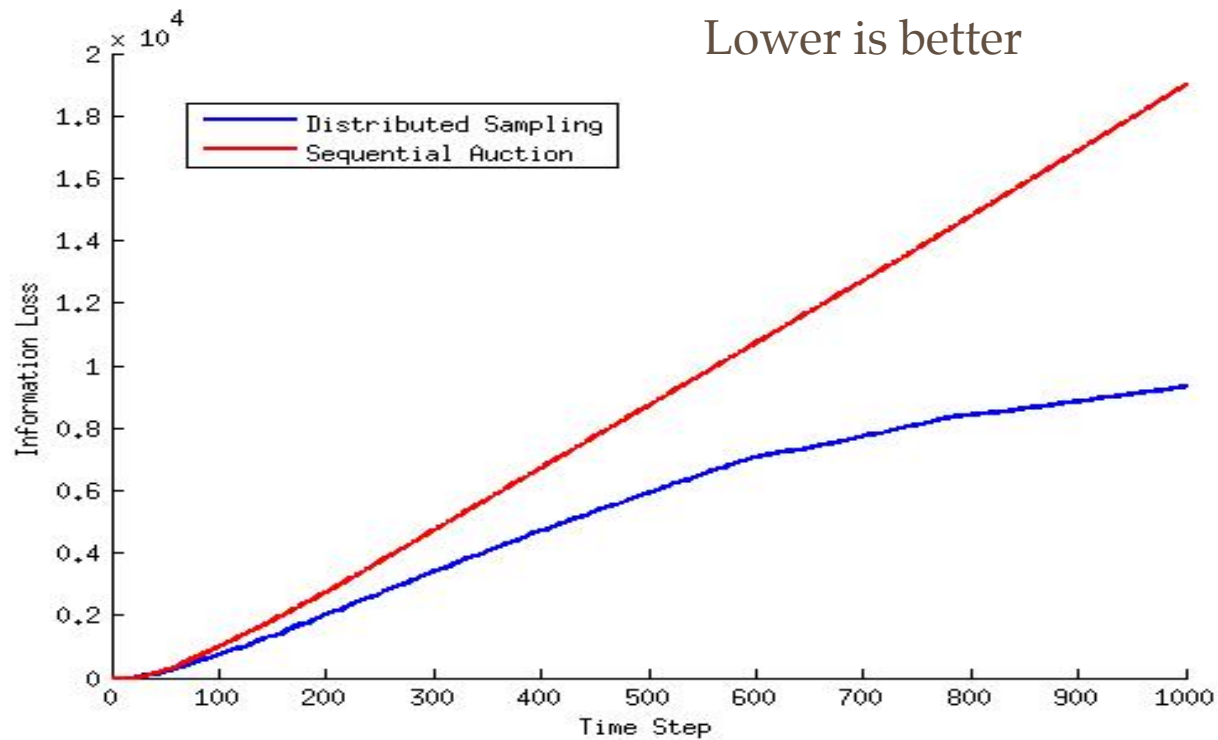
- 10 x 10 cells. Each cell contains 200 units of information
- Collectors: 2 collectors with collecting rate 5, 3 collectors with rate 2, 5 collectors with rate 1.
- Capacity: Both robots and collectors have a capacity of 100 to store information.
- Robots start from different corners.



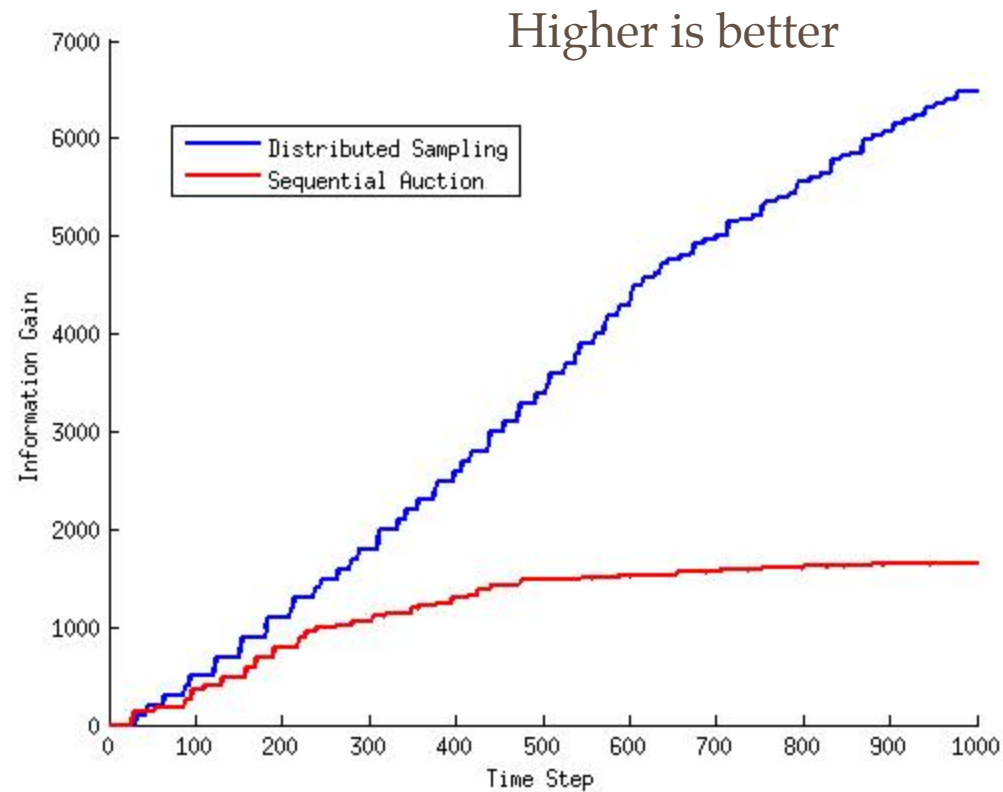
Idle Time (1000 steps)



Information Loss (1000 steps)



Information Gain (1000 steps)



Extension

Known environment vs. Unknown environment

- Certain vs. Uncertain

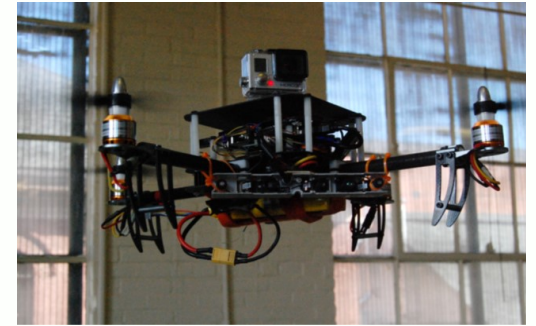
Global communication vs. Limited Communication

- Centralized vs. Decentralized

Multi-UAV Explore, Map, And Search in Unknown Environments



Introduction

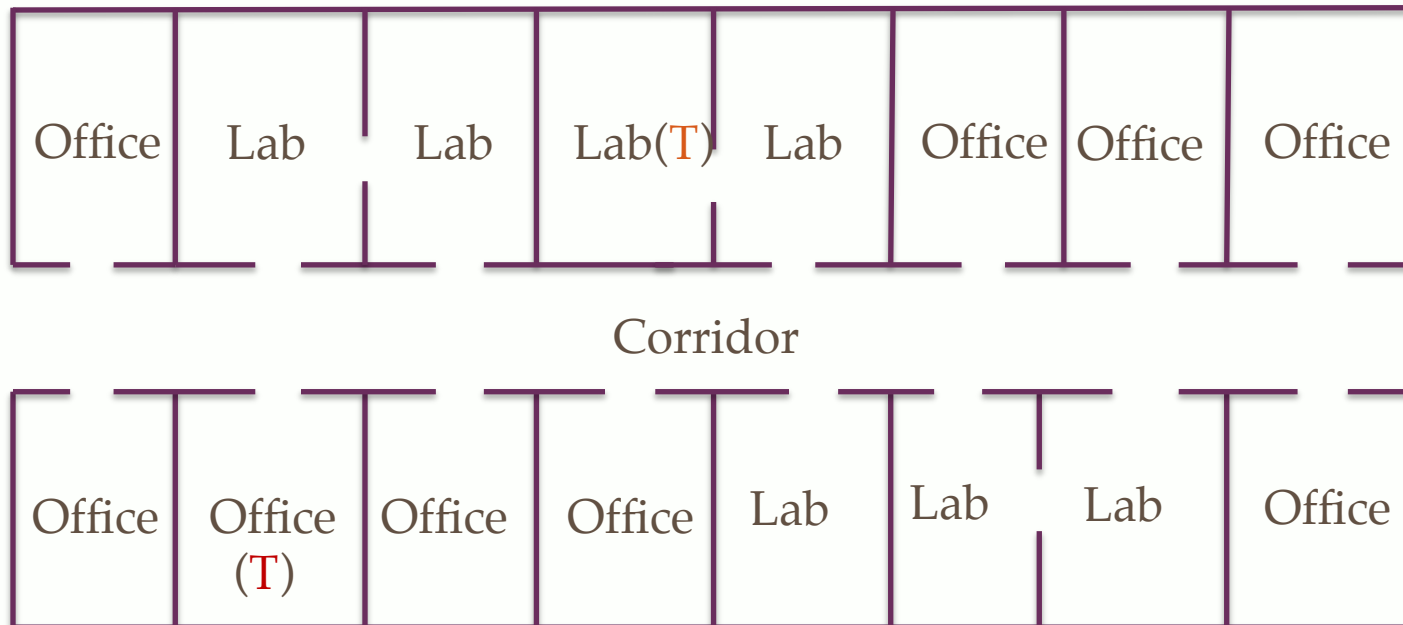


Goals

- An approach enable a team of UAVs simultaneously explore, map, and search in unknown environments.
- A mechanism controls the UAVs more focus on one or two sub-tasks (exploration, mapping and search) .
- A communication scheme efficiently the human operators during the mission.

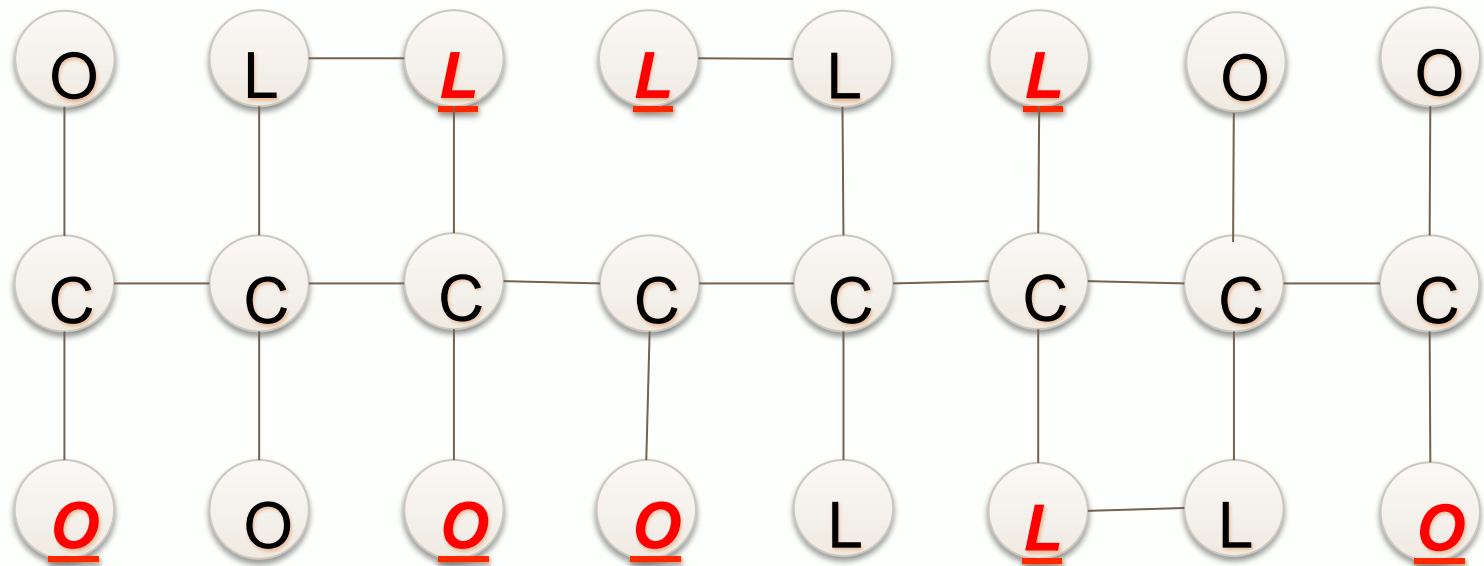
Problem Setup

- Environment
 - Indoor Environment with different types of rooms
 - Some rooms contain targets



Problem Setup

- Topological Representation
 - Model the environment as a graph with rooms as nodes



UAV Model

- Limited Battery Life
- Equipped with two types of sensors:
 - Observe the room type
 - Observe the target existence
 - Both of the sensors have noise
- Limited communication (disk model)

UAV Belief State

- Room type (assume UAVs know the all types of rooms)

For room r , probability of room type:

$$P \downarrow r = [P \downarrow t1, P \downarrow t2, \dots P \downarrow tn] \quad (n = |R|)$$

$$\sum_i P \downarrow ti = 1$$

- Target existence

For room r , probability of target existence

$$P \downarrow t = [P \downarrow T, P \downarrow F]$$

$$P \downarrow T + P \downarrow F = 1$$

Priors

- Priors provide the probability of a specific type room contains a target.

Office	Lab	Corridor
0.6	0.7	0.1

Bayesian Update

- Bayesian Update

- $P(R \uparrow t+1 | T) = P(T | R) / P(T) P(R \uparrow t)$

- $P(T \uparrow t+1 | R) = P(R | T) / P(R) P(T \uparrow t)$

- The posteriors become the new priors.

Reward Function

Robots choose one of the three actions:

- Visit a neighbor node (exploring)

$$I \downarrow E = I \alpha \uparrow \text{visited} \quad (I \text{ is the utility of first visit, } 0 < \alpha < 1)$$

- Observe for room type (mapping)

$$I \downarrow m = - \sum_{r \in R} P \downarrow r \log P \downarrow r$$

- Observe for target (search)

$$I \downarrow s = T \downarrow, T \in [0,1] \quad (\text{real utility gain})$$

$$I \downarrow s = P \downarrow T, P \downarrow T \in [0,1] \quad (\text{estimation})$$

Weighted Sub-goals

Weights are set up to more focus on one or two sub-tasks

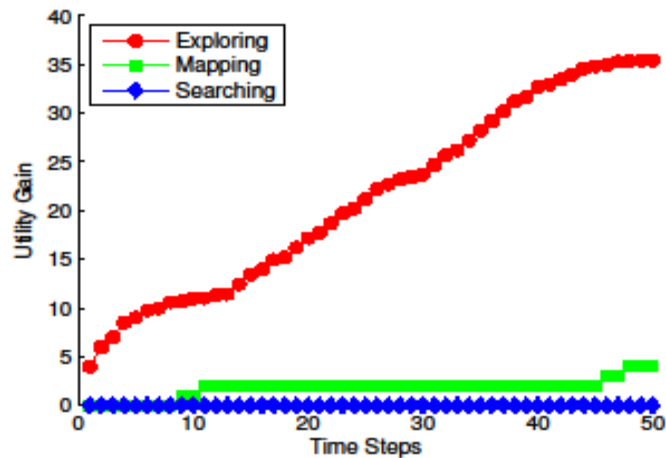
$$\omega = [\omega \downarrow e, \omega \downarrow m, \omega \downarrow s]$$

$$\omega \downarrow e + \omega \downarrow m + \omega \downarrow s = 1$$

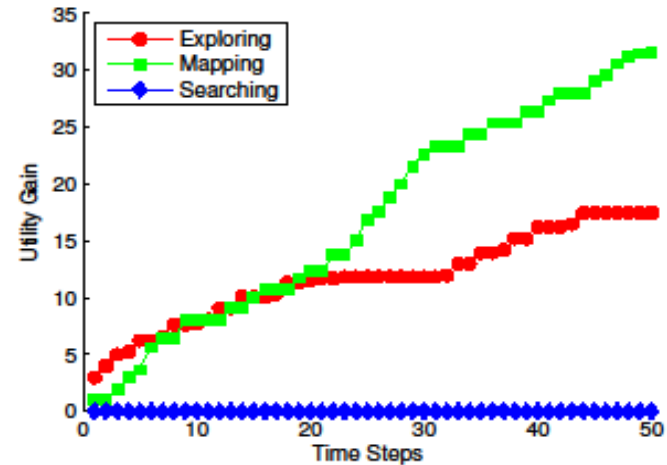
How to apply:

use ω times the estimated reward to generate new estimated reward

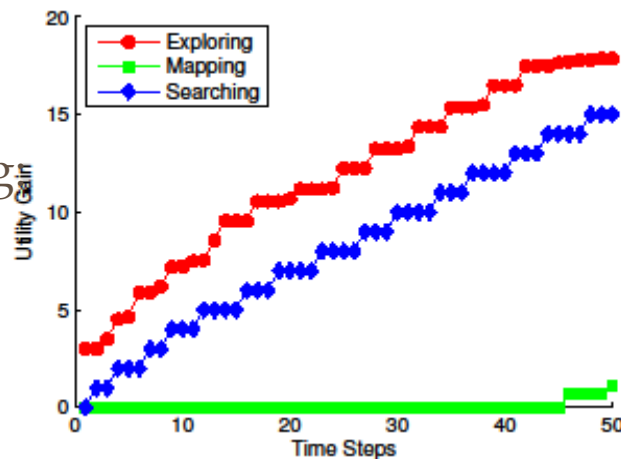
Results



Exploring: 0.9 Mapping:
0.05 Search: 0.05



Exploring: 0.05 Mapping:
0.9 Search: 0.05



Exploring: 0.05 Mapping:
0.05 Search: 0.9

Communication Loss Constraint

A communication loss constraint S is set up that only allows each UAV lose a valid communication link with human operators no more than S steps.

Idea: Engage the human operators **during** the mission

Algorithm: Baseline

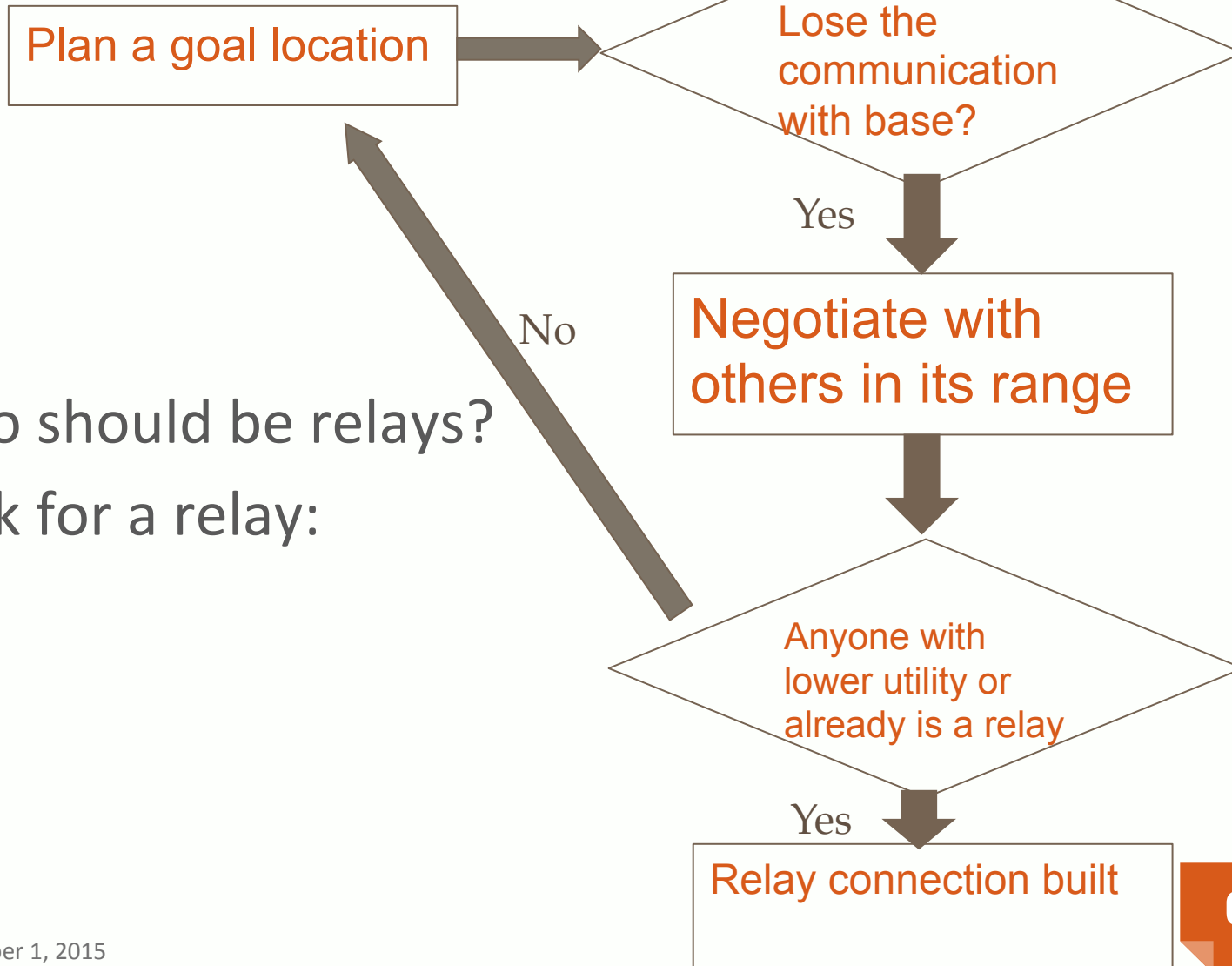
- Each UAV selects the action with the best estimated reward.
- Change if conflict with other UAVs with higher estimated reward for the same action.
- Have to select the goals without violate the constraint. Communicate with **base station** (human operators) at least every S steps.

Algorithm: ST-EMS (**S**teiner **T**ree – **E**xplore, **M**ap, **S**earch)

Explorer and Relay

- Explorer : explore, map, and search the environment base on the reward functions and weights.
- Relay: retrieve the explorer's information to base station so explorers have more freedom to fulfill the missions.

Algorithm: ST-EMS



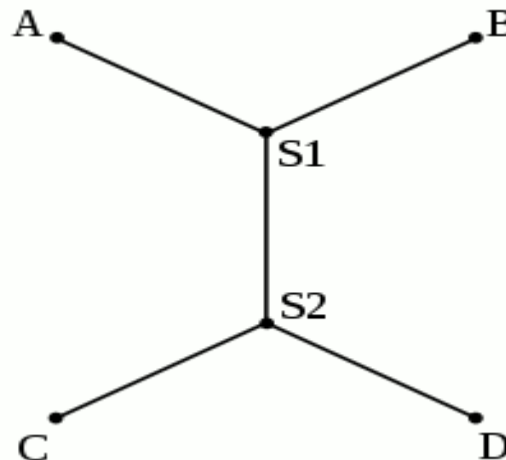
Who should be relays?
Look for a relay:

Algorithm: ST-EMS

- Find relay locations: Steiner Minimum Tree with Minimum Steiner Points and bounded edge length(*SMT-MSP*)

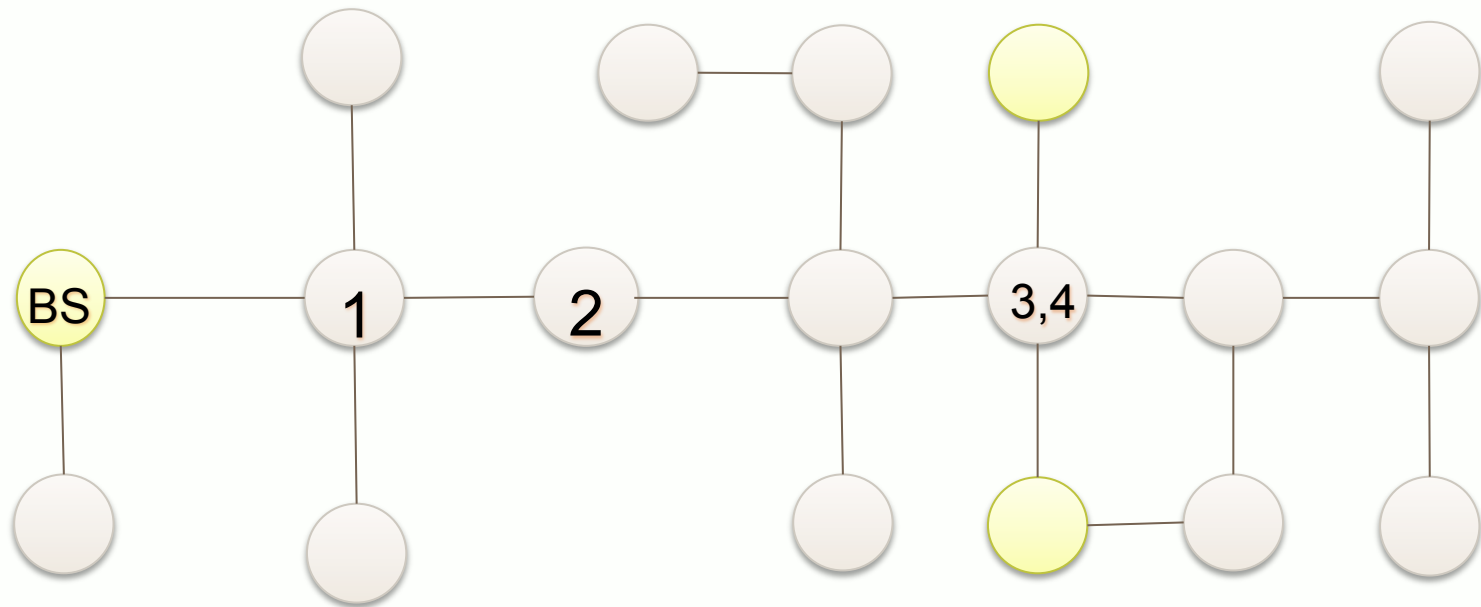
- Steiner Minimum Tree

Given a set V of vertices, interconnect them by a graph of shortest length



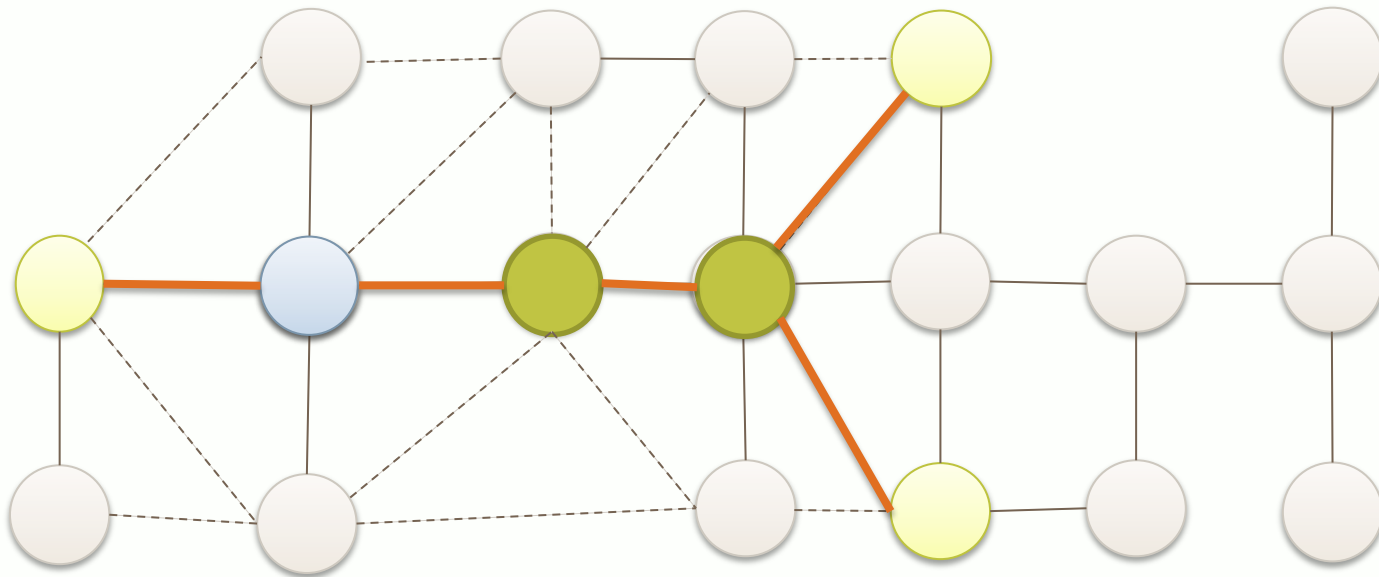
Algorithm: ST-EMS

- *SMT-MSP*
 - *Find the best relay locations*

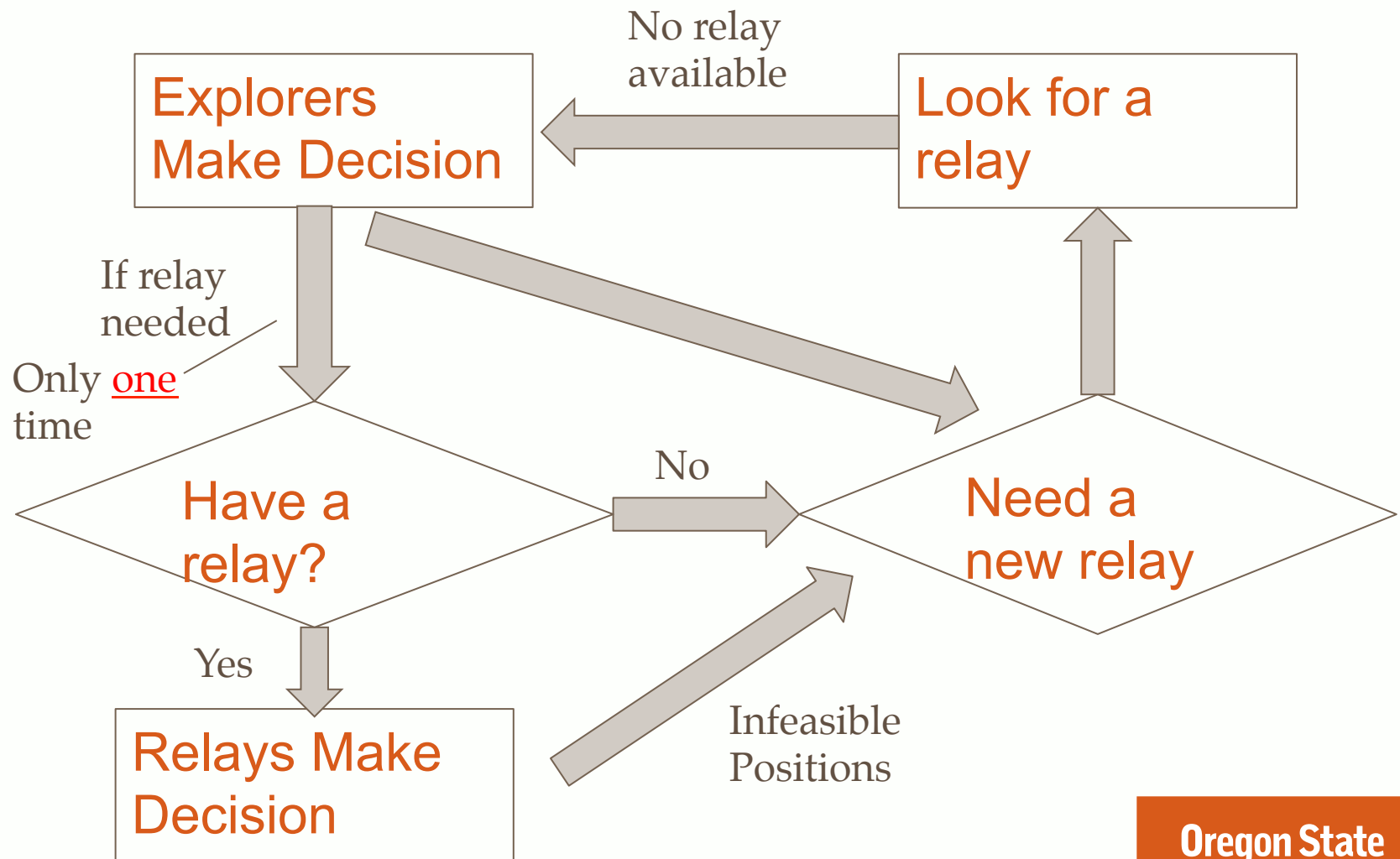


Algorithm: ST-EMS

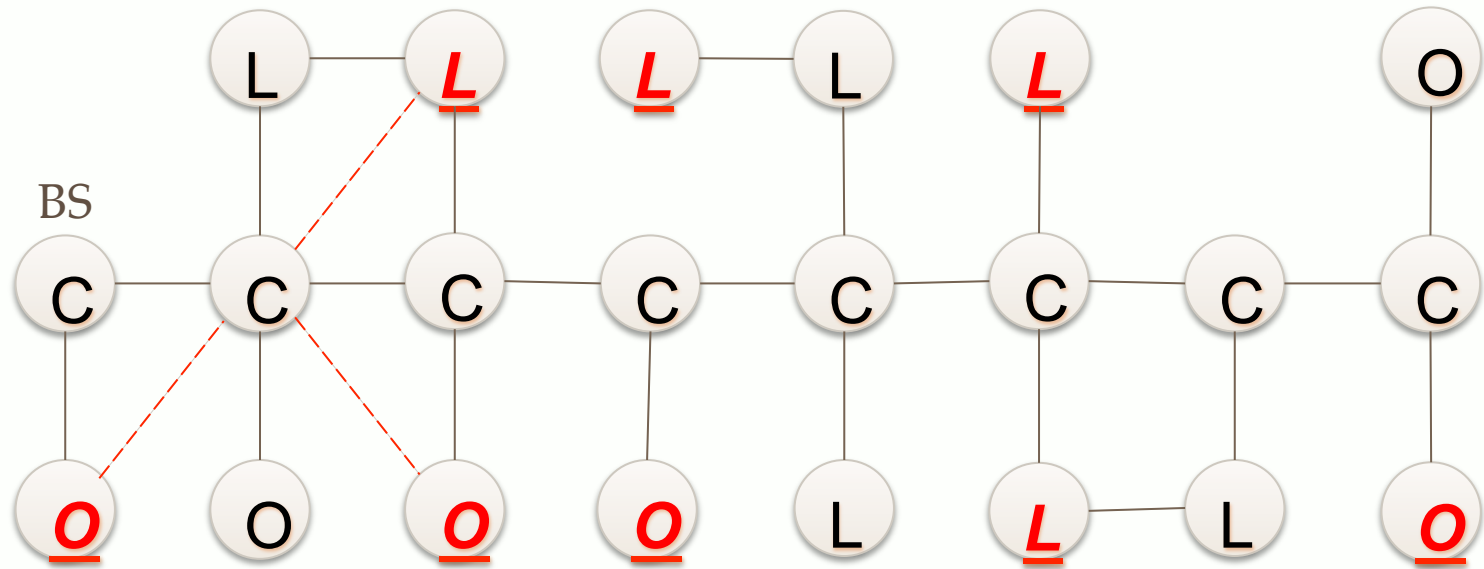
- SMT-MSP is NP-hard (Chen et. al, 2000)
- Greedy approximate (Du and Hu, 2008)



Algorithm: ST-EMS

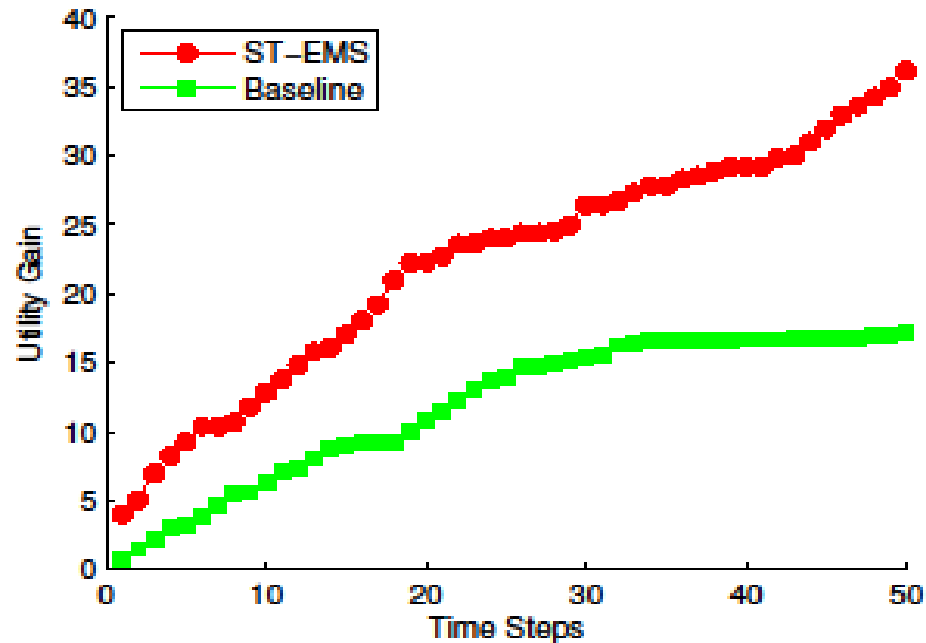


Simulation : Environment



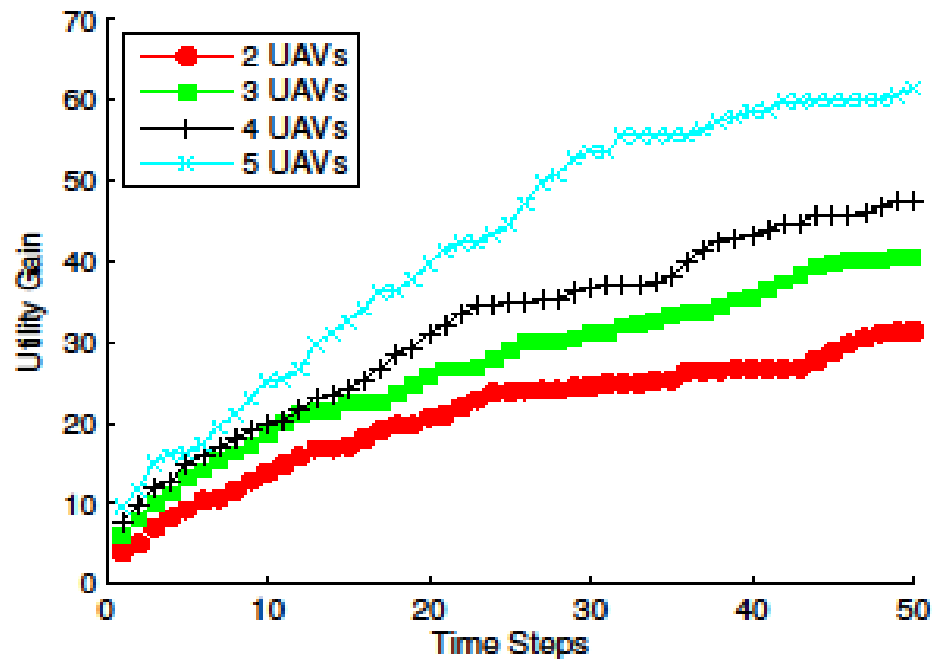
Results

- Total reward gain for both algorithms for 50 steps



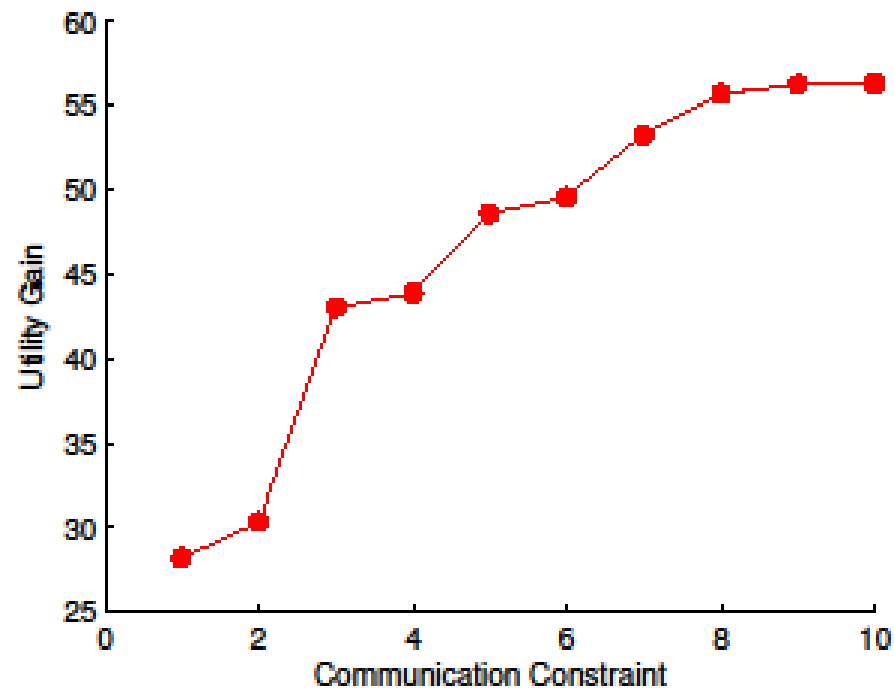
Results

- Scalability: total reward gain for 50 steps



Results

- Reward along with different communication loss constraint

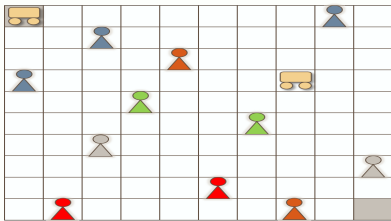


Summary of Contributions

- Known Environment with Global Communication:

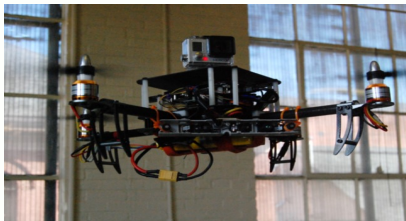


An intelligent in orchard auction-based bin-management system



Dynamic information gathering with even workload distribution and RH-based routing

- Unknown Environment with Limited Communication:



Multi-UAV Explore, Map, and Search simultaneously with operator preferences and communication loss constraint

Conclusion

Multi-robot coordination is difficult because:

- Large state space
- Many action choices
- Dynamic environments

We approach them by:

- Estimating a finite horizon of future changes
- Each robot makes independent decisions while contributing to a common objective
- Underlying representation allows coordination

Future Work

- Improved future predictions
 - Environment, task, teammates
- Better task decomposition and allocation
 - More sophisticated partitioning, Steiner tree approximation
- Integration with human operators
 - Learning operator preferences across environments
- Implementation: orchard bin management, UAV exploration/mapping/search

Acknowledgement



Center for Precision &
Automated Agricultural Systems
World Preeminent, Washington Relevant

WASHINGTON STATE  UNIVERSITY

Questions?

